

<u>MATHEMATICS OF CLASS X</u> <u>CHAPTER – 7 COORDINATE</u> <u>GEOMETRY</u>

Q.1. Find the distance between the following pairs of points:

(i) (2, 3), (4, 1) (ii) (-5, 7), (-1, 3) (iii) (a, b), (- a, - b)

Q.2. Find the distance between the points (0, 0) and (36, 15). Can you now find the distance between the two towns A and B discussed in Section 7.2.

Q.3. Determine if the points (1, 5), (2, 3) and (-2, -11) are collinear.

Q.4. Check whether (5, -2), (6, 4) and (7, -2) are the vertices of an isosceles triangle.

Q.5. In a classroom, 4 friends are seated at the points A, B, C and D as shown in the following figure. Champa and Chameli walk into the class and after observing for a few minutes Champa asks Chameli, "Don't you think ABCD is a square?" Chameli disagrees. Using distance formula, find which of them is correct.

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and give reasons for your answer:

(i) (-1, -2), (1, 0), (-1, 2), (-3, 0)

(ii)
$$(-3, 5), (3, 1), (0, 3), (-1, -4)$$

(iii) (4, 5), (7, 6), (4, 3), (1, 2)

Q.7. Find the point on the *x*-axis which is equidistant from (2, -5) and (-2, 9).

Q.8. Find the values of y for which the distance between the points P (2, -3)

and Q (10, y) is 10 units.

Q.9. If Q (0, 1) is equidistant from P (5, -3) and R (x, 6), find the values of x. Also find the distance QR and PR.

Q.10. Find a relation between x and y such that the point (x, y) is equidistant from the point (3, 6) and (-3, 4).

Q.11. Find the coordinates of the point which divides the join of (-1, 7) and (4, -3) in the ratio 2:3.

Q.12. Find the coordinates of the points of trisection of the line segment joining (4, -1) and (-2, -3).



Q.13. To conduct Sports Day activities, in your rectangular shaped school ground ABCD, lines have been drawn with chalk powder at a distance of 1 m each. 100 flower pots have been placed at a distance of 1 m from each other along AD, as shown in the following figure.

Niharika runs $\frac{1}{4}$ th the distance AD on the 2nd line and posts a green flag. Preet runs $\frac{1}{5}$ th the distance AD on the eighth line and posts a red

flag. What is the distance between both the flags? If Rashmi has to post a blue flag exactly halfway between the line segment joining the two flags, where should she post her flag?



Q.14. Find the ratio in which the line segment joining the points (-3, 10) and (6, -8) is divided by (-1, 6).

Q.15. Find the ratio in which the line segment joining A (1, -5) and B (-4, 5) is divided by the *x*-axis. Also find the coordinates of the point of division.

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Q.16. If (1, 2), (4, *y*), (*x*, 6) and (3, 5) are the vertices of a parallelogram taken in order, find *x* and *y*.

Q.17. Find the coordinates of a point A, where AB is the diameter of circle whose centre is (2, -3) and B is (1, 4)

Q.18. If A and B are (-2, -2) and (2, -4), respectively, find the coordinates

of P such that $AP = \frac{3}{7}AB$ and P lies on the line segment AB.

Q.19. Find the coordinates of the points which divide the line segment joining A (-2, 2) and B (2, 8) into four equal parts.

Q.20. Find the area of a rhombus if its vertices are (3, 0), (4, 5), (-1, 4) and (-

2, -1) taken in order. [Hint:Area of a rhombus = $\frac{1}{2}$ (product of its diagonals)]

Q.21. Find the area of the triangle whose vertices are:

(i) (2, 3), (-1, 0), (2, -4) (ii) (-5, -1), (3, -5), (5, 2)

Q.22. In each of the following find the value of 'k', for which the points are collinear.

(i) (7, -2), (5, 1), (3, -k) (ii) (8, 1), (k, -4), (2, -5)

Q.23. Find the area of the triangle formed by joining the mid-points of the sides of the triangle whose vertices are (0, -1), (2, 1) and (0, 3). Find the ratio of this area to the area of the given triangle.

Q.24. Find the area of the quadrilateral whose vertices, taken in order, are (-4, -2), (-3, -5), (3, -2) and (2, 3)



Q.25. You have studied in Class IX that a median of a triangle divides it into two triangles of equal areas. Verify this result for \triangle ABC whose vertices are A (4, - 6), B (3, - 2) and C (5, 2)

Q.26. Determine the ratio in which the line 2x + y - 4 = 0 divides the line segment joining the points A(2, -2) and B(3, 7)

Q.27. Find a relation between x and y if the points (x, y), (1, 2) and (7, 0) are collinear

Q.28. Find the centre of a circle passing through the points (6, -6), (3, -7) and (3, 3).

Q.29. The two opposite vertices of a square are (-1, 2) and (3, 2). Find the coordinates of the other two vertices.

Q.30. The class X students of a secondary school in Krishinagar have been allotted a rectangular plot of land for their gardening activity. Saplings of Gulmohar are planted on the boundary at a distance of 1 m from each other. There is a triangular grassy lawn in the plot as shown in the following figure. The students are to sow seeds of flowering plants on the remaining area of the plot.





(i) Taking A as origin, find the coordinates of the vertices of the triangle. (ii) What will be the coordinates of the vertices of Δ PQR if C is the origin? Also calculate the areas of the triangles in these cases. What do you observe? Q.31. The vertices of a Δ ABC are A (4, 6), B (1, 5) and C (7, 2). A line is drawn to intersect sides AB and AC at D and E respectively, such that $\frac{AD}{AB} = \frac{AE}{AC} = \frac{1}{4}$. Calculate the area of the Δ ADE and compare it with the area of Δ ABC. (Recall Converse of basic proportionality theorem and Theorem 6.6 related to ratio of areas of two similar triangles)

Q.32. Let A (4, 2), B (6, 5) and C (1, 4) be the vertices of \triangle ABC.

(i) The median from A meets BC at D. Find the coordinates of point D.

(ii) Find the coordinates of the point P on AD such that AP: PD = 2:1

(iii) Find the coordinates of point Q and R on medians BE and CF respectively such that BQ: QE = 2:1 and CR: RF = 2:1.

(iv) What do you observe?

(v) If $A(x_1, y_1)$, $B(x_2, y_2)$, and $C(x_3, y_3)$ are the vertices of $\triangle ABC$, find the coordinates of the centroid of the triangle.

Q.33. ABCD is a rectangle formed by the points A (-1, -1), B (-1, 4), C (5, 4) and D (5, -1). P, Q, R and S are the mid-points of AB, BC, CD, and DA respectively. Is the quadrilateral PQRS is a square? a rectangle? or a rhombus? Justify your answer.